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Modeling of operation regimes in coupled-cavity surface-emitting laser with external photon injection

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ABSTRACT

We present rate equation model of a modified vertical surface-emitting laser with two optical-coupled active cavities (CC-VSCEL) and external optical channel. The model allows to determine all the relevant parameters – carrier densities, gains, and output powers – starting from two input parameters: the injection currents in each cavity taking into account the additional external photonic injection. The system of rate equations is solved for different operating regimes of the modified laser device. The results provided by the model shown that operating characteristics of CC-VCSEL greatly depend on the number of photons of the external injection.

Keywords: coupled-cavity VCSELs, rate equation model, multisection device

1. INTRODUCTION

One of the limiting factors in the development of the photonic computing systems was the imperfection of diode laser emission. In vertical-cavity surface-emitting lasers (VCSEL) the symmetric optical beam with low divergence was obtained, single-mode generation regime with low threshold current and fast response (\geq 10Gbit/sec) is realized¹⁻⁴. The technology of CC-VCSEL became the improvement of VCSEL, where optical bistability is realized, taking into account modes polarization in generation regime of two laser emission wavelengths⁵⁻¹⁰. Its implementation has good prospects for the creation of the planar structures with great number of individually and coupled addressable emitters CC-VCSEL. It enables to create 2D data arrays in the form of the beams of phase-coupled coherent polarized emission within specialized photon devices for matrix calculations¹⁰⁻¹².

2. AIM OF THE RESEARCH

In the given research, on the base of rate equations for the hypothetically modified structure of CC-VCSEL with the external photon injection, suggested in¹¹ simulation study of the characteristics of the device for operating stationary regimes with different input and output parameters of the model is performed, taking into consideration the impact of the amount of the external photons in the cavity and realized by means of computer algebra system Mathcad 15.

3. RATE EQUATION FOR CC-VCSEL WITH THE PHOTON INJECTION

We will consider the CC-VCSEL, formed by two optically coupled active cavities, scheme of which is suggested in^{10,11}. The structure of CC-VCSEL with the hypothetical channel for the additional photon injection (for instance, for data transmission) is shown in Fig. 1¹⁰. Technological aspects of channel formation and the parameters of its emission we will leave aside the dissension in the given research^{13–15}.

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Figure 1. Structure of CC-VCSEL with the external photon injection

Rate equation CC-VCSEL were obtained on the base of the model of photon-reservoirs, suggested by V. Badilita and coauthors in^{7,10,16}. The equations are modified for CC-VCSEL with the hypothetical external photon injection in^{10,11,17}.



Figure 2. Model of the photon-reservoirs of CC-VSCEL with the external optical injection¹⁰

In the model of the photonic-reservoirs (Fig. 2), the limited volume V_i with a certain number of carriers N_i (i = 1 - top cavity, i = 2 - bottom cavity) is allocated to each of the structures zones, numbers of the photons in each mode are determined for the photon-reservoirs N_{pi}^s and N_{pi}^L (S – short, L – long mode), correspondingly. Designations in Fig. 2: I/q – carriers injection rate of the laser; η_i – carriers injection efficiency reaching the active region; $R_{mi}V_i$ – rate of non-radiative recombination; $R_{spi}V_i$ – rate of spontaneous recombination. Additionally external optical wave with the number of photons N_{pi}^{ext} in each photon reservoirs is present (we conventionally assume the number of external photons in each cavities to be equal: $N_{pi}^{ext} = N_{p2}^{ext} = N_p^{ext}$).

Rate equations for the carriers and photons for CC-VCSEL with external injection are written as follows¹¹:

$$\frac{\eta_{1}I_{1}}{q} = A_{1}^{S} \cdot N_{p}^{S} \cdot g_{1}^{S} + A_{1}^{L} \cdot N_{p}^{L} \cdot g_{1}^{L} + A_{1}^{ext} \cdot N_{p}^{ext} \cdot g_{1}^{ext} + \frac{N_{1}}{\tau_{e}},$$
(1)

$$\frac{\eta_2 I_2}{q} = A_2^S \cdot N_p^S \cdot g_2^S + A_2^L \cdot N_p^L \cdot g_2^L + A_2^{ext} \cdot N_p^{ext} \cdot g_2^{ext} + \frac{N_2}{\tau_e},$$
(2)

$$N_{p}^{s} \cdot \left(A_{1}^{s} \cdot g_{1}^{s} + A_{2}^{s} \cdot g_{2}^{s} - \frac{1}{\tau_{p}^{s}} \right) = 0 , \qquad (3)$$

$$N_{p}^{L} \cdot \left(A_{1}^{L} \cdot g_{1}^{L} + A_{2}^{L} \cdot g_{2}^{L} - \frac{1}{\tau_{p}^{L}} \right) = 0 , \qquad (4)$$

$$N_{p}^{ext} \cdot \left(A_{1}^{ext} \cdot g_{1}^{ext} + A_{2}^{ext} \cdot g_{2}^{ext} - \frac{1}{\tau_{p}^{ext}} \right) = 0 , \qquad (5)$$

where $g_i^{S,L,ext} = G_0^{S,L,ext} \cdot \ln \frac{n_i + n_0^{S,L,ext}}{n_v^{S,L,ext}}$ – is the gain coefficient for the modes *S*, *L* and external mode in the cavity *i*, $n_i = N_i / V_i$ – is carrier density in the quantum wells, $n_v^{S,L}$ – is the transparency carrier density in the cavity, which corresponds to zero gain, $n_0^{S,L,ext}$ determines the quantum well absorption at the corresponding wavelength; $A_i^{S,L} = 2\xi_i^{S,L} \frac{l_i}{L} \Gamma_i^{S,L}$, $A_i^{ext} = 2\xi_i^{ext} v^{ext} \Gamma_i^{ext}$ – are the constants containing the design parameters of the device. In this case $v_g^{S,L,ext}$ – is the group velocity of the photons in each of the modes, $V_{p,i}$ – is the volume of the photon reservoir *i*, $\xi_i^{S,L,ext}$ – is the standing wave enhancement factor (varies between 0 and 2, depending on the quantum wells in the field)¹⁸⁻²⁰.

Equation systems (1) – (5) contains seven unknown parameters: number of photons N_p^s , N_p^L and N_p^{ext} , number of carriers N_1 and N_2 , injection currents I_1 and I_2 . Having set any two of the seven parameters as "input parameters", the system of equations can be solved with the respect to the remaining five unknowns^{21–23}.

4. SIMULATION OF THE OPERATING REGIMES OF CC-VCSEL WITH THE PHOTON INJECTION

In the work^{7,10} such operation regimes of CC-VSCEL device are considered (such regimes will be take place if the additional external photon channel is available):

A. The "double-threshold" point (point where both modes start lasing simultaneously);

B. The mode lasing threshold, if the other mode remains below thresholds value;

C. One mode lasing threshold if the order mode is above the threshold value;

D. One mode lasing far above the threshold value, if the value of other mode is below the threshold value;

E. Both modes have the values above the threshold.

For each of the above mentioned regimes the values of the corresponding injection currents must be interconnected to fulfill the lasing conditions. We will simulate the operation of our device in each of the regimes separately.

4.1 Case A. The "double-threshold" point

It is the point where lasing starts simultaneously for both modes, that is why the number of photons for each of the optic modes in the corresponding cavities 1 and 2 is zero: $N_p^S = 0$, $N_p^L = 0$.

The number of photons of the external emission N_p^{ext} is considered to be input parameter for modeling. The output parameters of the study we consider simulation dependences: $I_1(N_p^{ext})$, $I_2(N_p^{ext})$.

Taking into account the above-mentioned conditions the equations (1)-(5) can be writer in such form (for simplification we assume that the transparency carrier's density in the cavities is the same $n_{tr}^{s} = n_{tr}^{L} = n_{tr}$)¹¹:

$$\frac{\eta_1 I_1}{q} = A_1^{ext} \cdot G_0^{ext} \cdot \ln\left(\frac{\frac{N_1}{V_1} + n_0^{ext}}{n_{tr} + n_0^{ext}}\right) \cdot N_p^{ext} + \frac{N_1}{\tau_e}$$
(6)

$$\frac{\eta_2 I_2}{q} = A_2^{ext} \cdot G_0^{ext} \cdot \ln\left(\frac{\frac{N_2}{V_2} + n_0^{ext}}{n_{tr} + n_0^{ext}}\right) \cdot N_p^{ext} + \frac{N_2}{\tau_e}, \qquad (7)$$

$$A_{1}^{S} \cdot G_{0}^{S} \cdot \ln\left(\frac{\frac{N_{1}}{V_{1}} + n_{0}^{S}}{n_{rr} + n_{0}^{S}}\right) + A_{2}^{S} \cdot G_{0}^{S} \cdot \ln\left(\frac{\frac{N_{2}}{V_{2}} + n_{0}^{S}}{n_{rr} + n_{0}^{S}}\right) = \frac{1}{\tau_{p}^{S}},$$
(8)

$$A_{1}^{L} \cdot G_{0}^{L} \cdot \ln\left(\frac{N_{1}}{V_{1}} + n_{0}^{L}}{n_{tr} + n_{0}^{L}}\right) + A_{2}^{L} \cdot G_{0}^{L} \cdot \ln\left(\frac{N_{2}}{V_{2}} + n_{0}^{L}}{n_{tr} + n_{0}^{L}}\right) = \frac{1}{\tau_{p}^{L}},$$
(9)

$$A_{1}^{ext} \cdot G_{0}^{ext} \cdot \ln\left(\frac{\frac{N_{1}}{V_{1}} + n_{0}^{ext}}{n_{tr} + n_{0}^{ext}}\right) + A_{2}^{ext} \cdot G_{0}^{ext} \cdot \ln\left(\frac{\frac{N_{2}}{V_{2}} + n_{0}^{ext}}{n_{tr} + n_{0}^{ext}}\right) = \frac{1}{\tau_{p}^{ext}}.$$
(10)

We will introduce the following designations: $v_{\log i}^{S,L} = \ln\left(\frac{\frac{N_{i,0}}{V_i} + n_0^{S,L}}{n_{tr} + n_0^{S,L}}\right), v_{\log i}^{ext} = \ln\left(\frac{\frac{N_{i,0}}{V_i} + n_0^{ext}}{n_{tr} + n_0^{ext}}\right).$

Solving the system of equations (8)-(9) as the linear system, we obtain the expression for the number of carriers in double-threshold point $N_{i,0}$ in each of the cavities:

$$N_{i,0}^{S,L} = \left[\left(n_{tr}^{S,L} + n_0^{S,L} \right) \exp\left(\nu_{\log i}^{S,L} \right) - n_0^{S,L} \right] V_i \quad .$$
(11)

Using same input parameters for simulation as the authors in¹⁰ (Table 1), such values for the number of carriers and their density in double-threshold point for S – mode lasing

$$v_{\log i}^{ext} = \begin{pmatrix} 0,083\\ 0,071 \end{pmatrix}, \quad \begin{pmatrix} N_{1,0}\\ N_{2,0} \end{pmatrix} = \begin{cases} 8,314 \cdot 10^6\\ 3,966 \cdot 10^6 \end{cases}, \quad \begin{pmatrix} n_{1,0}^s\\ n_{2,0}^s \end{pmatrix} = \begin{cases} 2,598 \cdot 10^{18}\\ 2,479 \cdot 10^{18} \end{cases} cm^{-1}.$$

Density of the photons of the external injection n_0^{ext} , at which the conditions of the double-threshold point are satisfied, we determined further from the expression (10), substituting in it instead of N_1 and N_2 the values of the numbers of carriers, obtained above for S – mode $N_{1,0}$ and $N_{2,0}$: $n_0^{ext} = 7,3645 \cdot 10^{18} cm^{-1}$.

Parameter	Physical quantities	Value
Standing wave enhancement factor	$\xi_1^S, \xi_1^L, \xi_1^{ext}$	1,63
	$\xi_2^S, \xi_2^L, \xi_2^{ext}$	1,92
Confinement coefficient	Γ_1^S , Γ_2^L	0,76
	Γ_1^S , Γ_2^L	0,24
	Γ_1^{ext}	0,4
	Γ_2^{ext}	0,6
Gain coefficient (cm ⁻¹)	$G_0^{\scriptscriptstyle S}$, $G_0^{\scriptscriptstyle ext}$	1800
	G_0^L	2000
Volume of the cavity (m ³)	$V_1 \\ V_2$	$3,2 \cdot 10^{-12} \\ 1,6 \cdot 10^{-12}$
Group velocity (m/s)	V_g^S, V_g^L, V_g^{ext}	7,894·10 ⁹
Photon lifetime (ps)	$ au_p^S$	0,289
	$ au_p^L$, $ au_p^{ext}$	0,257
Carrier escape time (ps)	$ au^e$	1
Carriers injection efficiency	η_{1} , η_{2}	0,8
Carriers density in the quantum wells (cm ⁻¹)	n_0^S , n_0^L n_0^{ext}	0,4.1018
Transparency carrier density (cm ⁻¹)	n_{tr}^{S} , n_{tr}^{L}	1,8.1018
Cavity width (cm)	l_1, l_2	0,24.10-4

Table1. Input parameters of CC-VCSEL for modeling



Figure 3. Dependence of the double-threshold point of CC-VCSEL on the injection currents (mA) if $N_p^{ext} = 0 \dots 10^7$

Further, taking into account the obtained values $N_{1,0}$ and $N_{2,0}$, we solve the system of linear equations (6)-(7) respectively injection currents of the double-threshold point as the function from the number of the photons N_p^{ext} of the external injection for each of the cavities for S – mode:

$$I_{point 1}(N_{p}^{ext}) = \frac{q}{\eta_{1}} (A_{1}^{ext} \cdot G_{0}^{ext} \cdot v_{\log_{1}}^{ext} \cdot N_{p}^{ext} + \frac{N_{1,0}}{\tau_{e}}),$$

$$I_{point 2}(N_{p}^{ext}) = \frac{q}{\eta_{2}} (A_{2}^{ext} \cdot G_{0}^{ext} \cdot v_{\log_{2}}^{ext} \cdot N_{p}^{ext} + \frac{N_{2,0}}{\tau_{e}})$$
(12)

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The analysis of the resent studies shows that the position of the "double-threshold" point depends on the number of the external photons linearly. Its position on the directed line is determined from the expression (Fig. 3):

$$I_{point 2} = k_x I_{point 1} + k_y = \frac{\eta_1}{\eta_2} \frac{A_2^{ext} \cdot V_{\log_2}^{ext}}{A_1^{ext} \cdot V_{\log_1}^{ext}} I_{point 1} + const .$$
(13)

Taking into consideration the parameters of model $k_x = 1,512$. The results of the simulation for L-mode are analogous.

4.2 Case B. Borders of the "one-mode lasing" regions

In this regime the lasing conditions for one of the modes are not valid (since its value is under threshold values).

East we simulate the operation of L-mode for the case, when the value of S-mode is under the threshold values. In the system of rate equations, taking into account the external photon injection the equation (8) is not valid²⁴.

As the output, thus in *Case A*, we have $N_p^S = N_p^L = 0$.

We will simulated the dependence $I_2(I_1, N_p^{ext})$.

In this case the equation (9) can be written

$$N_{2}(N_{1}) = \left[(n_{tr} + n_{0}^{L}) \exp\left(\frac{-A_{1}^{L}}{A_{2}^{L}} \ln\left(\frac{N_{1}}{V_{1}} + n_{0}^{L}\right) + \frac{1}{A_{2}^{L} \tau_{p}^{L} G_{0}^{L}}\right) - n_{0}^{L} \right] V_{2}.$$
(14)

The solution of the non-linear equation (6) will be done in Mathcad 15 package using the Lambert is *W*-function. After a set of mathematical transformations we obtain the dependence of the number of carriers in the second cavity on the injection current in the first cavity and a number of the external photons for the *L*-mode:

$$N_{2}^{L}(I_{I}, N_{p}^{ext}) = \left[(n_{tr} + n_{0}^{L}) \exp\left(\frac{-A_{1}^{L}}{A_{2}^{L}} \ln\left(\frac{\frac{N_{1B}(I_{I}, N_{p}^{ext})}{V_{1}} + n_{0}^{L}}{n_{tr} + n_{0}^{L}}\right) + \frac{1}{A_{2}^{L} \tau_{p}^{L} G_{0}^{L}} - n_{0}^{L} \right] V_{2},$$
(15)

where

$$\begin{split} N_{1B}(I_{I}, N_{p}^{ext}) &= V_{1} \left[(n_{tr} + n_{0}^{L}) \left(\frac{1}{\beta(N_{p}^{ext})} W \left[\beta(N_{p}^{ext}) e^{\alpha(I_{I}, N_{p}^{ext})} \right] \right] - n_{0}^{ext} \right] \\ \beta(N_{p}^{ext}) &= \frac{V_{1}(n_{tr} + n_{0}^{ext})}{A_{1}^{ext} \tau_{e} G_{0}^{ext} N_{p}^{ext}}; \\ \alpha(I_{I}, N_{p}^{ext}) &= \frac{1}{A_{1}^{ext} G_{0}^{ext} N_{p}^{ext}} \left(\frac{\eta_{1}}{q} I_{1} + \frac{n_{0}^{ext} V_{1}}{\tau_{e}} \right). \end{split}$$

Substituting (15) into (7) we obtain the expression of the target output dependence for *L*-mode

$$I_{2B}^{L}(I_{1}, N_{p}^{ext}) = \frac{q}{\eta_{2}} \left[A_{2}^{ext} G_{0}^{ext} N_{p}^{ext} \ln \left(\frac{\frac{N_{2}^{L}(I_{1}, N_{p}^{ext})}{V_{2}} + n_{0}^{ext}}{n_{tr} + n_{0}^{ext}} \right) + \frac{N_{2}^{L}(I_{1}, N_{p}^{ext})}{\tau_{e}} \right]$$
(16)

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In the same way we obtain the output dependence for S-mode in the regime, if L-mode is below the threshold (in the system of rate equation the equation (7) is not valid).

The expression of the target output dependence for S-mode (L-mode is under the threshold):

$$I_{2B}^{s}(I_{1}, N_{p}^{ext}) = \frac{q}{\eta_{2}} \left| A_{2}^{ext} G_{0}^{ext} N_{p}^{ext} \ln \left(\frac{\frac{N_{2}^{s}(I_{1}, N_{p}^{ext})}{V_{2}} + n_{0}^{ext}}{n_{tr} + n_{0}^{ext}} \right) + \frac{N_{2}^{s}(I_{1}, N_{p}^{ext})}{\tau_{e}} \right|$$
(17)

Graphs in Fig. 4 illustrate the obtained dependences for each of mutually exclusive in the given regime S and L modes, taking into account the imposer constraints at the external injection of photons in the range of $N_p^{ext} = 1 \cdot 10^1 ... 5 \cdot 10^5$.



Figure 4. Calculated dependences of the threshold point on the injection currents for Case B if $N_p^{ext} = 1.10^1 \dots 5.10^5$

4.3 Case C. Borders of the "both modes lasing" regions

In this mode two variants of the operation are possible:

1. Lasing of S- mode at the threshold of L-mode ($N_p^L = 0$ and $N_p^S > 0$);

2. Lasing of *L*-mode at the threshold of *S*-mode ($N_p^S = 0$ and $N_p^L > 0$).

In each of the variants the corresponding output characteristic is simulated $I_2(I_1, N_p^{ext})$.

We will consider the first variant of the operation.

The solutions of the system of rate equations (3)-(4) for this case by analogy with *Case A* have the form (12). The solution of the system of linear equations (1)-(2) for *S*-mode in this case has the form:

$$I_{2C}^{S}\left(I_{1}, N_{p}^{ext}\right) = \frac{\eta_{1}}{\eta_{2}} \frac{A_{2}^{S} V_{\log 2}^{S}}{A_{1}^{S} v_{\log 1}^{S}} \left[I_{1} - \frac{q}{\eta_{1}} \left(\frac{N_{1,0}}{\tau_{e}} + A_{1}^{ext} G_{0}^{ext} v_{\log 1}^{ext} N_{p}^{ext}\right)\right] + \frac{q}{\eta_{2}} \left(\frac{N_{2,0}}{\tau_{e}} + A_{2}^{ext} G_{0}^{ext} v_{\log 2}^{ext} N_{p}^{ext}\right).$$
(18)

The analysis of the formula shows that this function for *S*-mode changes linearly from the number of the external photons with the constant angular factor (for the parameters, set in the model it equals 3,241).

For the second variant (lasing of *L*-mode) the solution is found analogous:

$$I_{2C}{}^{L}\left(I_{1}, N_{p}^{ext}\right) = \frac{\eta_{1}}{\eta_{2}} \frac{A_{2}^{L} v_{\log 2}^{L}}{A_{1}^{L} v_{\log 1}^{L}} \left[I_{1} - \frac{q}{\eta_{1}} \left(\frac{N_{1,0}}{\tau_{e}} + A_{1}^{ext} G_{0}^{ext} v_{\log 1}^{ext} N_{p}^{ext}\right)\right] + \frac{q}{\eta_{2}} \left(\frac{N_{2,0}}{\tau_{e}} + A_{2}^{ext} G_{0}^{ext} v_{\log 2}^{ext} N_{p}^{ext}\right).$$
(19)

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Similarly, this function for *L*-mode changes linearly from the number of external photons with the constant angular factor (for the parameters, set in the model it equals 0,323).

Analyzing the obtained solutions we make the conclusions that:

- 1. Position of the "double-threshold" point depending on the number N_p^{ext} changes linearly,
- 2. Threshold values of modes S and L lasing are linearly.

Calculated dependences of the functions (18) and (19) on injection currents under the emission of the external photons in the range of values $N_p^{ext} = 1.10^5 ... 9.10^6$ are shown in Fig. 5.



Figure 5. Calculation dependences of the injection currents functions in the cavities for the injection of the external photons in the range of $N_p^{ext} = 1 \cdot 10^5 ... 9 \cdot 10^6$

4.4 Case D. Inside the one-mode lasing regions

The solution of rate equations for CC-VSCEL with the account of the external photons injection in this regime using the Lambert's *W*-function is not possible (only by the numerical methods).

4.5 Case E. Inside the dual-mode lasing regions

Within the range of this operation regime two variants are considered:

- 1. $N_p^L = const$, $N_p^S > 0$,
- 2. $N_p^{S} = const$ and $N_p^{L} > 0$.

We will consider $I_2(I_2, N_p^{ext}, N_p^L)$ and $I_2(I_2, N_p^{ext}, N_p^S)$ as the output characteristic, correspondingly.

The solution of the equations (3)-(4) is considered in *Case A*, *C*. By analogy, the following dependences are obtained for variant 1:

$$I_{2E}^{S}\left(I_{1}, N_{p}^{ext}, N_{p}^{L}\right) = \frac{\eta_{1}}{\eta_{2}} \frac{A_{2}^{S} v_{\log 2}^{S}}{A_{1}^{S} v_{\log 1}^{S}} \left[I_{1} - \Delta I_{1}^{S} \left(N_{p}^{ext}, N_{p}^{L}\right) + \Delta I_{2}^{S} \left(N_{p}^{ext}, N_{p}^{L}\right)\right],$$
(20)

where:

$$\Delta I_{1}^{S}(N_{p}^{ext}, N_{p}^{L}) = \frac{q}{\eta_{1}} \left(\frac{N_{1,0}}{\tau_{e}} + A_{1}^{ext} G_{0}^{ext} \nu_{\log 1}^{ext} N_{p}^{ext} + A_{1}^{L} G_{0}^{L} \nu_{\log 1}^{L} N_{p}^{L} \right),$$

$$\Delta I_2^S(N_p^{ext}, N_p^L) = \frac{q}{\eta_1} \left(\frac{N_{2,0}}{\tau_e} + A_2^{ext} G_0^{ext} v_{\log 2}^{ext} N_p^{ext} + A_2^L G_0^L v_{\log 2}^L N_p^L \right).$$

For variant 2 the analogous (20) expressions are obtained:

$$I_{2E}^{\ L}\left(I_{1}, N_{p}^{ext}, N_{p}^{S}\right) = \frac{\eta_{1}}{\eta_{2}} \frac{A_{2}^{L} v_{\log 2}^{L}}{A_{1}^{L} v_{\log 1}^{L}} \Big[I_{1} - \Delta I_{1}^{L} (N_{p}^{ext}, N_{p}^{S}) + \Delta I_{2}^{L} (N_{p}^{ext}, N_{p}^{S})\Big],$$
(21)

where

$$\Delta I_{1}^{L}(N_{p}^{ext}, N_{p}^{S}) = \frac{q}{\eta_{1}} \left(\frac{N_{1,0}}{\tau_{e}} + A_{1}^{ext} G_{0}^{ext} V_{\log 1}^{ext} N_{p}^{ext} + A_{1}^{S} G_{0}^{S} V_{\log 1}^{S} N_{p}^{S} \right),$$

$$\Delta I_{2}^{L}(N_{p}^{ext}, N_{p}^{S}) = \frac{q}{\eta_{1}} \left(\frac{N_{2,0}}{\tau_{e}} + A_{2}^{ext} G_{0}^{ext} V_{\log 2}^{ext} N_{p}^{ext} + A_{2}^{S} G_{0}^{S} V_{\log 2}^{S} N_{p}^{S} \right).$$

Fig. 6 shows the calculations dependences of lasing threshold point for all the regimes taking into account *Case E* (excluding *Case D*) at $N_p^{ext} = 10^4$, $N_p^S = N_p^L = 10^6$.



Figure 6. Calculation dependences of CC-VSCEL injection currents with the external photon injection, taking into account the thresholds for *Cases A, B, C, E* at $N_p^{ext} = 10^4$, $N_p^S = N_p^L = 10^6$

Graphs in Fig. 6 illustrate the obtained dependences for *S* and *L* modes in regimes *A*, *B*, *C*, *E* of CC-VCSEL operation, taking into account the parameters of the model (Table 1).

5. CONCLUSIONS

In the process of the investigation of operating regimes of CC-VCSEL with additional external photon injection in the cavity, it is shown that operating characteristics in the considered cases in stationary conditions greatly depend on the number of photons of the external injection. The analysis of the obtained analytical solutions allowed to make or conclusion regarding the character of the obtained dependences in basic working regimes of the laser multisection device. The results of the simulation can be useful for the development of basic modules of specialized photon systems for matrix computation^{9,11}.

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