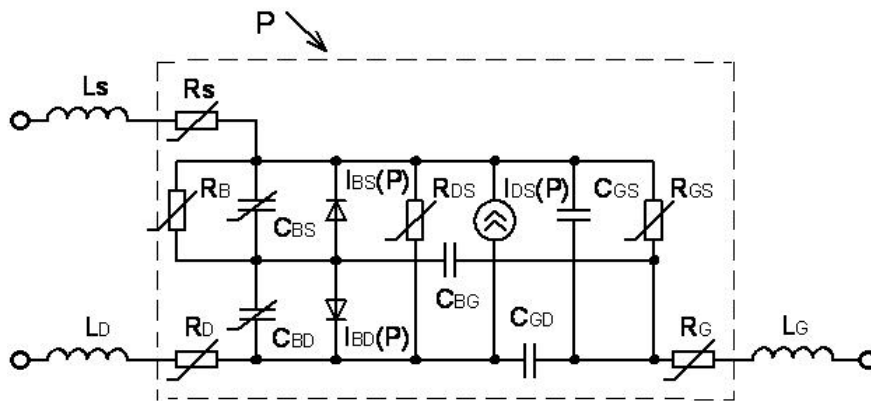


The paper presents a mathematical model of deformation effects in MOS transistor that is used as an element in tenzosensitive of pressure transducer with a frequency output . On the basis of a mathematical model designed dependence of the threshold voltage, saturation voltage, gate-source voltage of the pressure action. Most dependence of these parameters on the pressure observed at work MOS transistor in saturation at high pressures greater than 10^8 Pa.

Keywords: deformation effect, frequency sensor, tensor sensible element.

[1],



.1.

$$G_i = f(F_i(P))$$

$$\Delta G_i(P) = \frac{\partial G_i}{\partial F_i} \Delta F_i(P), \tag{1}$$

F_i -

$$G_i \tag{1}$$

: R_D - , R_S - , R_G - , R_B - , R_{DS} - , R_{GS} - , $C_{BS} = C_{BD}$ - () - .

$$I_{BD} = I_{DS} \left[\exp\left(\frac{V_{BD}}{V_t}\right) - 1 \right], \tag{2}$$

I_{DS} – p-n ; V_{BD} – ; V_t –

$$I_{DS} = A_D J_s + P_D J_{ssw}, \quad (3)$$

A_D – ; J_{ssw} – ; P_D – ; J_s –

$$J_s = qZN_{A(D)} / \quad [3]: \quad (4)$$

q – ; Z – ; $N_{A(D)}$ –

$$Z^2 = D, \quad [4] \quad (5)$$

D –

$$D = kT\mu/q. \quad (6)$$

k – ; – ; ~ –

$$J_s = N_{A(D)} \left(\frac{qkT\mu}{2} \right)^{\frac{1}{2}}, \quad (7)$$

$$J_{ssw} = P_{LD} N_{A(D)} \left(\frac{qkT\mu}{2} \right)^{\frac{1}{2}}, \quad (8)$$

P_{LD} –

$$\frac{dI_{DS}}{dP} = I_{DS} \left(\frac{\Delta N_{A(D)}(P)}{N_{A(D)}} + \frac{\Delta\mu(P)}{\mu} \right). \quad (9)$$

$$\frac{dI_{BD}}{dP} = I_{BD} \left(\frac{\Delta N_{A(D)}(P)}{N_{A(D)}} + \frac{\Delta\mu(P)}{\mu} \right). \quad (10)$$

$$I_{BS} = I_{SS} \left[\exp\left(\frac{V_{BS}}{V_t}\right) - 1 \right]. \quad (11)$$

V_{BS} – ; I_{SS} – p-n

$$I_{SS} = A_S J_s + P_S J_{ssw}, \quad (12)$$

A_S – ; P_S –

$$\frac{dI_{BS}}{dP} = I_{BS} \left(\frac{\Delta N_{A(D)}(P)}{N_{A(D)}} + \frac{\Delta\mu(P)}{\mu} \right). \quad (13)$$

$$I_D = I_{drain} - I_{BD}. \quad (14)$$

$$\frac{dI_D}{dP} = \frac{dI_{drain}}{dP} - \frac{dI_{BD}}{dP}. \quad (15)$$

[2]

$$I_S = -I_{drain} - I_{BS}. \quad (16)$$

$$\frac{dI_S}{dP} = -\frac{dI_{drain}}{dP} - \frac{dI_{BS}}{dP}. \quad (17)$$

$$I_{drain} = \begin{cases} 0 & (V_{GS} - V_{to} < 0), \\ \frac{V_{DS} [V_{GS} - V_{to} - 0,5(1 + F_b)V_{DS}]}{[1 + V_{DS}\mu_{eff}/(L_{eff}V_{max})]} & (0 < V_{GS} - V_{to} < V_{DS}) \end{cases} \quad [5]: \quad (18)$$

$$\Delta I_{drain}(P) = \frac{\partial I_{drain}}{\partial V_{to}} \Delta V_{to}(P) + \frac{\partial I_{drain}}{\partial F_b} \Delta F_b(P) + \frac{\partial I_{drain}}{\partial V_{GS}} \Delta V_{GS}(P) + \frac{\partial I_{drain}}{\partial \mu_{eff}} \Delta \mu_{eff}(P) + \frac{\partial I_{drain}}{\partial L_{eff}} \Delta L_{eff}(P), \quad (19)$$

$$\frac{\partial I_{drain}}{\partial V_{to}} \Delta V_{to}(P) = -\frac{V_{DS}}{[1 + V_{DS}\mu_{eff}/(L_{eff}V_{max})]} \Delta V_{to}(P); \quad (20)$$

$$\frac{\partial I_{drain}}{\partial F_b} \Delta F_b(P) = -\frac{0,5 V_{DS}^2}{[1 + V_{DS}\mu_{eff}/(L_{eff}V_{max})]} \Delta F_b(P); \quad (21)$$

$$\frac{\partial I_{drain}}{\partial V_{GS}} \Delta V_{GS}(P) = \frac{V_{DS}}{[1 + V_{DS}\mu_{eff}/(L_{eff}V_{max})]} \Delta V_{GS}(P); \quad (22)$$

$$\frac{\partial I_{drain}}{\partial \mu_{eff}} \Delta \mu_{eff}(P) = -\frac{V_{DS}^2 L_{eff} V_{max}}{[1 + V_{DS}\mu_{eff}]^2} \Delta \mu_{eff}(P); \quad (23)$$

$$\frac{\partial I_{drain}}{\partial L_{eff}} \Delta L_{eff}(P) = \frac{V_{DS} [V_{GS} - V_{to} - 0,5(1 + F_b)V_{DS}]}{[1 + V_{DS}\mu_{eff}/(L_{eff}V_{max})]} \Delta L_{eff}(P); \quad (24)$$

$$\frac{\partial I_{drain}}{\partial L_{eff}} \Delta L_{eff}(P) = \frac{S_{eff} V_{DS}^2 [V_{GS} - V_{to} - 0,5(1 + F_b)V_{DS}]}{L_{eff}^2 V_{max} [1 + V_{DS}\mu_{eff}/(L_{eff}V_{max})]^2} \Delta L_{eff}(P), \quad (25)$$

$$F_b - ; \sim_{eff} - ; L_{eff} - ; V_{to} - ; V_{max} - .$$

[2]:

$$= \frac{0,5 K_p W}{L}, \quad (26)$$

$$W - ; L - ; K_p -$$

$$K_p = u_0 C_{ox}, \quad (27)$$

$$u_0 - ; C_{ox} - ; T_{ox} = e_{ox} / T_{ox}, \quad (28)$$

$$e_{ox} - ; T_{ox} - .$$

$$= \frac{0,5u_0 e_{ox} W}{T_{ox} L} \quad (29)$$

$$\Delta (P) = \frac{0,5e_{ox} W}{T_{ox} L} \cdot \Delta u_0(P), \quad (30)$$

$$\Delta u_0(P) = V_{GS} \quad [5]:$$

$$V_{GS} = W_{GS} + V_{GS0}, \quad (31)$$

$$\frac{dV_{GS}}{dP} = \frac{dW_{GS}}{dP} \quad (32)$$

$$W_{GS} = V_t \ln \frac{p_p n_n}{n_i^2}, \quad (33)$$

$$\Delta V_{GS}(P) = W_{GS} \left(\frac{\Delta p_p(P)}{p_p} + \frac{\Delta n_n(P)}{n_n} - \frac{2\Delta n_i(P)}{n_i} \right) \quad (34)$$

$$V_{to} = V_{to0} - u V_{DS} + x F_s (W - V_{BS})^{1/2} + F_n (W - V_{BS}) + V_t x_N, \quad (35)$$

$$V_{to0} - ; V_{DS} - ; x - ; u - ; F_s - ; V_{BS} - ; F_n - ; x_N - ; \{ -$$

$$V_{to0} = V_{bi} \pm xW^{1/2}, \quad (36)$$

$$V_{bi} = W_s - 10^4 q N_{ss} / C_{ox}, \quad (37)$$

$$W_s = W_g - (F_p + 0,5E_g + 3,25), \quad (38)$$

$$W_s = 3,2B, \quad W_s = 3,25 + E_g$$

$$W_s = 3,25B -$$

$$F_p = \pm \{ / 2 - ($$

$$); E_g - ; u,$$

[3] :

$$u = \frac{8,15 \cdot 10^{-22} y}{C_{ox} L_{eff}^3}, \quad (39)$$

$$y = 1 + \frac{0,25f de_{sil} T_{ox}}{e_{ox} W}, \quad (40)$$

$$\chi = \frac{(2 \cdot 10^6 e_{sil} q N_{sub})^{\frac{1}{2}}}{C_{ox}}, \quad (41)$$

[4]:

$$w = 2V_t \ln \left(\frac{10^4 N_{ss}}{n_i} \right), \quad (42)$$

[2]:

$$F_n = \frac{f de_{sil}}{2C_{ox} W}. \quad (43)$$

[3]:

$$x_N = 1 + \frac{10^4 q N_{fs}}{C_{ox}} + \frac{\chi F_s (W - V_{BS})^{\frac{1}{2}} + F_n (W - V_{BS})}{2(W - V_{BS})}, \quad (44)$$

$$\Delta V_{to}(P) = \frac{\partial V_{to}}{\partial E_g} \Delta E_g(P) + \frac{\partial V_{to}}{\partial F_p} \Delta F_p(P) + \frac{\partial V_{to}}{\partial N_{sub}} \Delta N_{sub}(P) + \frac{\partial V_{to}}{\partial e_{sil}} \Delta e_{sil}(P) + \frac{\partial V_{to}}{\partial n_i} \Delta n_i(P) + \frac{\partial V_{to}}{\partial N_{ss}} \Delta N_{ss}(P), \quad (45)$$

$$\frac{\partial V_{to}}{\partial E_g} \Delta E_g(P) = -\frac{1}{2} \Delta E_g(P); \quad (46)$$

$$\frac{\partial V_{to}}{\partial F_p} \Delta F_p(P) = -\Delta F_p(P); \quad (47)$$

$$\frac{\partial V_{to}}{\partial N_{sub}} \Delta N_{sub} = \frac{\chi}{2N_{sub}} \left[F_s (W - V_{BS})^{\frac{1}{2}} \left(1 + \frac{V_t}{2(W - V_{BS})} \right) \pm W^{\frac{1}{2}} \right] \Delta N_{sub}(P); \quad (48)$$

$$\frac{\partial V_{to}}{\partial n_i} \Delta n_i(P) = -\frac{V_t}{n_i} \left(\frac{\chi F_s}{(W - V_{BS})^{\frac{1}{2}}} + 2F_n \pm \frac{\chi}{W^{\frac{1}{2}}} - \frac{\chi F_s V_t}{2(W - V_{BS})^{\frac{3}{2}}} \right) \Delta n_i(P); \quad (49)$$

$$\frac{\partial V_{to}}{\partial e_{sil}} \Delta e_{sil}(P) = \frac{1}{e_{sil}} \left(\frac{\chi F_s}{2(\chi - V_{BS})^{1/2}} - \frac{u(y - e_{sil})}{y} + F_n(\chi - V_{BS}) + \frac{V_t}{2} \left(\frac{\chi F_s V_t}{2(\chi - V_{BS})} + F_n \right) \right) \Delta e_{sil}(P). \quad (50)$$

$$\frac{\partial V_{to}}{\partial N_{ss}} \Delta N_{ss} = \frac{V_t}{N_{ss}} \left(\left[\frac{\chi F_s}{(W - V_{BS})^{1/2}} \pm \frac{\chi}{W^{1/2}} + 2F_n + \frac{V_t}{(W - V_{BS})^2} \right] \times \left[\left(\frac{\chi F_s}{2(W - V_{BS})^{1/2}} + F_n \right) (W - V_{BS}) - \left[-\chi F_s (W - V_{BS})^{1/2} - F_n (W - V_{DS}) \right] \right] - \frac{10^4 q}{C_{ox}} \right) \Delta N_{ss}(P); \quad (51)$$

F_b

[2]:

$$F_b = F_n + \frac{F_s}{2(W - V_{BS})^{1/2}}, \quad (52)$$

:

$$\Delta F_b(P) = \frac{\partial F_b}{\partial e_{sil}} \Delta e_{sil}(P) + \frac{\partial F_b}{\partial N_{sub}} \Delta N_{sub}(P) + \frac{\partial F_b}{\partial n_i} \Delta n_i(P) + \frac{\partial F_b}{\partial N_{ss}} \Delta N_{ss}(P). \quad (53)$$

C

(53)

:

$$\frac{\partial F_b}{\partial e_{sil}} \Delta e_{sil}(P) = \frac{1}{e_{sil}} \left(F_n + \frac{F_s}{4(W - V_{BS})^{1/2}} \right) \Delta e_{sil}(P); \quad (54)$$

$$\frac{\partial F_b}{\partial N_{sub}} \Delta N_{sub}(P) = \frac{F_s}{4N_{sub}(W_{BS} - V_{BS})^{1/2}} \Delta N_{sub}(P); \quad (55)$$

$$\frac{\partial F_b}{\partial n_i} \Delta n_i(P) = \frac{F_s V_t}{2n_i(W - V_{BS})^{3/2}} \Delta n_i(P); \quad (56)$$

$$\frac{\partial F_b}{\partial N_{ss}} \Delta N_{ss}(P) = -\frac{F_s V_t}{2N_{ss}(W - V_{BS})^{3/2}} \Delta N_{ss}(P). \quad (57)$$

[2]:

$$\mu_{eff} = u_0 \mu_{fact}, \quad (58)$$

u_0 -

; μ_{fact} -

$$\mu_{fact} = \frac{1}{(1 + (V_{GS} - V_{to}))}, \quad (59)$$

" -

(58),

$$\mu_{eff} = u_0 / (1 + (V_{GS} - V_{to})). \quad (60)$$

$\Delta \mu_{eff}(P)$

:

$$\Delta \mu_{eff}(P) = \mu_{eff} \left(\frac{\Delta u_0(P)}{u_0} - \frac{\Delta V_{GS}(P)}{(1 + (V_{GS} - V_{to}))} + \frac{\Delta V_{to}(P)}{(1 + (V_{GS} - V_{to}))} \right). \quad (61)$$

$$V_{DS} \leq V_{DSsat} \quad L_{eff} \quad L_{eff} = L, \\ \Delta L_{eff}(P) = 0 \text{ [2].} \quad V_{DS} > V_{DSsat} \text{ [2]:}$$

$$L_{eff} = L - L_{\Delta}, \quad (62)$$

$$L_{\Delta} \quad L_1 = \sqrt{A + B^2} < 0,5L \quad : \\ L_{\Delta} = x_d \left[A + B^2 \right]^{1/2}, \quad (63)$$

$$x_d - \quad \left(\quad \right) \\ x_d = \left(\frac{2e_{sil}}{10^6 q N_{sub}} \right)^{1/2}; \quad A = t(V_{DS} - V_{DSsat}), \quad (64)$$

$$\chi - \quad ; V_{DSsat} - \quad ; \\ B = 0,5V_{max} x_d \left(1 + LV_{max} / (V_{DS} \sim_{eff}^2) \right). \quad (65)$$

$$L_{eff} \quad : \\ L_{eff} = L - x_d \left[t(V_{DS} - V_{DSsat}) + 0,25V_{max}^2 x_d^2 \left(1 + LV_{max} / (V_{DS} \sim_{eff}^2) \right)^2 \right]^{1/2}. \quad (66)$$

$$\Delta L_{eff}(P) = \frac{1}{2} \left[L_{\Delta} + \frac{x_d^2 B^2}{L_{\Delta}} \right] \cdot \left[\frac{\Delta N_{sub}(P)}{N_{sub}} - \frac{\Delta V_{sil}(P)}{V_{sil}} \right] + \\ + \frac{x_d^2}{2L_{\Delta}} \left[t \Delta V_{DSsat}(P) + \frac{x_d L B V_{max}^2}{V_{ds} \sim_{eff}^3} \Delta \sim_{eff}(P) \right]. \quad (67)$$

$$L_1 > 0,5L \quad L_{\Delta} \quad : \\ L_{\Delta} = L - x_L \left(1 - 0,25x_L / x_d \left[A + B^2 \right]^{1/2} \right), \quad (68)$$

$$(64) \quad (65): \\ L_{\Delta} = L - x_L \left(1 - \frac{0,25x_L}{x_d \left[t(V_{DS} - V_{DSsat}) + 0,25V_{max}^2 x_d^2 \left(1 + LV_{max} / (V_{DS} \sim_{eff}^2) \right)^2 \right]} \right). \quad (69)$$

$$L_{eff} \quad : \\ \Delta L_{eff}(P) = \frac{x_L^2}{8L_{\Delta}^2} \cdot \left(\left[L_{\Delta} + \frac{x_d^2 B^2}{L_{\Delta}} \right] \cdot \left[\frac{\Delta N_{sub}(P)}{N_{sub}} - \frac{\Delta V_{sil}(P)}{V_{sil}} \right] + \right. \\ \left. + \frac{x_d^2}{L_{\Delta}} \left[t \Delta V_{DSsat}(P) + \frac{x_d L B V_{max}^2}{V_{DS} \sim_{eff}^3} \Delta \sim_{eff}(P) \right] \right). \quad (70)$$

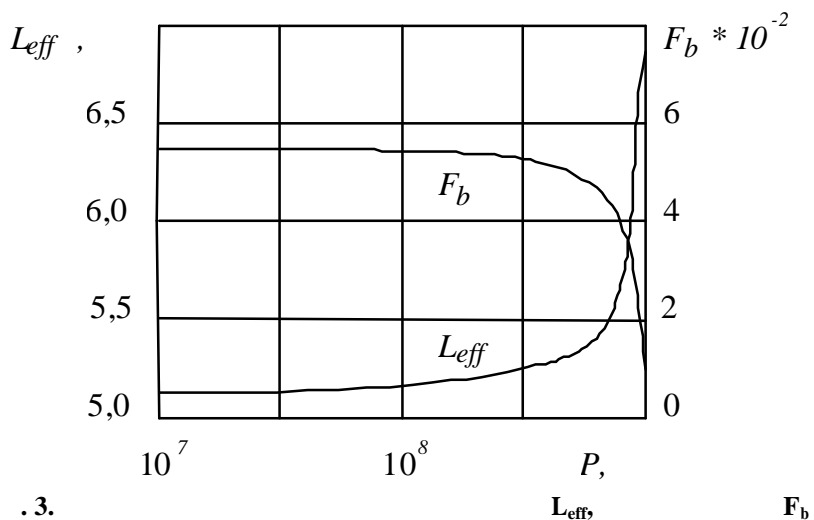
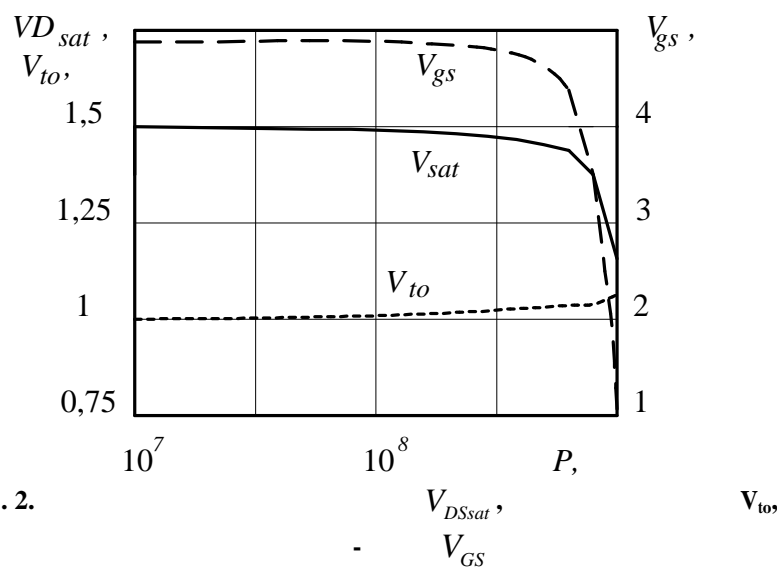
$$V_{DSsat} \text{ [1]} \quad : \\ V_{DSsat} = V_a + V_b - (V_a^2 + V_b^2)^{1/2}, \quad (71)$$

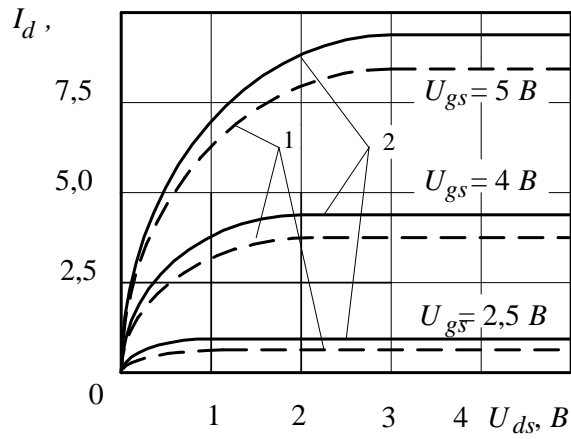
$$V_a = (V_{GS} - V_{to}) / (1 + F_b); \quad V_b = L_{eff} V_{max} / \tilde{\sim}_{eff} \cdot \quad [3]:$$

$$\Delta V_{DSsat}(P) = \frac{V_{dsat}}{(1 + F_b)} \left(\frac{V_a}{(V_a^2 + V_b^2)^{1/2}} - 1 \right) + V_b \left(\frac{\Delta \tilde{\sim}_{eff}(P)}{\tilde{\sim}_{eff}} - \frac{\Delta L_{eff}(P)}{L_{eff}} \right) \left(\frac{V_b}{(V_a^2 + V_b^2)^{1/2}} - 1 \right) \quad (72)$$

"MatLab 7.1" I_D

$$I_D(P) = I_{BD}(P) - I_{drain}(P) \quad (73)$$





.4. (1) (2)

1. , , , 10^8 , -
2. , , -
3. (10^8) -

1. 83354 , 01R 19/00. /
u201300303; .09.01.2013; .10.09.13. .17.
2. , . : 2- , .1/ .- .: ,1984.-456 .
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20.07.2013 .