

## LEARNING SCIENCE (AND MATHEMATICS) WITH MATHEMATICAL MODELLING: CAN STUDENTS LEARN BY DOING?

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Using computers as learning tools is becoming more and more common. There are many reasons for this, particularly those related to the fact that computers are a window to the networked world of information and knowledge. But in STEM subjects (Science, Technology, Engineering and Mathematics), and particularly in Physics, there are other reasons: computers are now an inevitable tool in the advancement of knowledge. Unfortunately, this is not yet true in most school curricula, where common practices still tend to reduce learning of STEM subjects to the rote accumulation of facts and rules, without emphasizing how knowledge and ideas are created and tested.

Physics is a key subject in the science and technology education curricula. In spite of such central role, introductory physics continues to be extremely difficult for students both at the secondary and at the university level. Due to a lack of understanding of fundamental concepts in physics and mathematics, the number of students unable to pass on course examinations is usually very high. What is worse is that many of those students that eventually succeed also reveal several weaknesses in their understanding of elementary physics.

Clearly, a solution for this problem requires changes in the processes by which science is taught and learnt. In recent years, many results of educational research have shown that the process of learning is effectively enhanced when students are involved in the learning activities as scientists are involved in research. Indeed, most scientific research is a dynamical process of creation, testing and improvement of mathematical models that describe observable physical phenomena. This process is an interactive blend of individual and group reflections based on a continuously evolving and mutually balanced set of theoretical, computational and experimental elements. It is from this cognitive frame of action that an inspiring understanding of the laws of the physical universe emerges. Hence, it should not be surprising that the process of learning science may turn out to be more successful in research inspired environments where students are helped to work as teams of scientists do. In this kind of class environment, knowledge performance is better promoted and common sense beliefs as well as incorrect scientific notions can be more effectively fought.

In the scientific research process, computational modelling plays an important role in the expansion of the cognitive horizon through more powerful calculation, exploration and visualization capabilities. Consequently, modelling with computational methods and tools is also an important aspect of research inspired learning environments. In this context, it is crucial to achieve an early integration of scientific computation in a way that is balanced with theory and experiment. Only then the learning and teaching processes can be in phase with modern scientific research, where computation is as important as theory and experiment, and with the rapid parallel development of technology.

Modelling in computer learning environments started with an emphasis on programming languages. Using, for example, Fortran, Pascal and, more recently, Python, this approach requires students to develop a working knowledge of programming. The same happens with scientific computation software such as Mathematica or Matlab. To avoid overloading students with programming notions and syntax, computer modelling systems such as Stella, Easy Java Simulations and Modellus were developed to focus the learning activities on the understanding of the concepts of science and mathematics.

Our group has been involved in creating scientific software that young students can use, without the complexities of professional tools. Modellus, a mathematical modelling package freely available (<http://modellus.fct.unl.pt>) is a product of that effort and which is now an integral part of curricula, such as Advancing Physics, in the UK (<http://advancingphysics.iop.org>). Modellus allows students to create and explore models based on functions, differential equations and iterations and its interface is specially designed to be used without extensive training on how to use it.

Modellus assumes that meaningful learning of abstract mathematical concepts, the key elements of scientific modelling, involves the reification of these concepts. The concepts of mathematics must be treated as real objects, as “objects-to-think-with”, as Seymour Papert wrote many years ago. And scientific software like Modellus allows students to treat mathematical objects as “concrete-abstract objects”: concrete in the sense they can be manipulated and visualized and abstract because they are mathematical constructs.

School curricula in STEM subjects, where computers are an integral part of the curricula, will, sooner or later, naturally incorporate modelling tools. This is not an easy task and the effort involved to make it will surely be long since it involves the development of new ideas, new curricular materials, professional development for teachers, dissemination of computers on school systems, changes in initial teacher education, etc. It is a difficult and long task, but it is not an impossible one, and certainly it will be accomplished as school systems and society increase the use of computers and computer networks on all aspects of the emergent “information society”.